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# Measuring Productivity

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**“Productivity isn’t everything  
but in the long run it is almost  
everything”**

Paul Krugman *The Age of  
Diminishing Expectations*

# 1. Why is productivity important?

- Basis for improvements in real incomes and economic well-being:
- Monetary policy (inflationary pressures)
- Fiscal policy (financing of health, education, welfare)
- Slow productivity growth = conflicting demands for distribution of income more likely

## 2. Concepts: labour productivity

- Every measure of productivity is a ratio between output and input(s)
- Simplest and most frequently-encountered measure: labour productivity:

$$\text{Labour productivity (LP)} = \frac{Q}{L}$$

- Indicates how efficiently labour is used in production
- Not necessarily an indicator of effort per worker

# Table of productivity measures

<i>Type of output measure:</i>	<i>Type of input measure</i>			
	<i>Labour</i>	<i>Capital</i>	<i>Capital &amp; labour</i>	<i>Capital, labour &amp; intermediate inputs (energy, materials, services)</i>
<i>Gross output</i>	Labour productivity (based on gross output)	Capital productivity (based on gross output)	Capital - labour MFP (based on gross output)	KLEMS multi-factor productivity
<i>Value-added</i>	Labour productivity (based on value-added)	Capital productivity (based on value-added)	Capital – labour MFP (based on value-added)	-
	<i>Single factor productivity measures</i>		<i>Multi-factor productivity (MFP) measures</i>	

## 2. Concepts: multi-factor productivity

- Ratio of output and combined capital and labour input

$$\text{Multi-factor productivity (MFP)} = \frac{Q}{F(L, K)}$$

- Indicates how efficiently combined labour and capital are used in production

- When measured as rate of change:

The diagram illustrates the decomposition of the rate of change in multi-factor productivity (MFP) into its components. The central equation is:

$$\ln\left(\frac{Q^t}{Q^{t-1}}\right) = s_L \ln\left(\frac{L^t}{L^{t-1}}\right) + s_K \ln\left(\frac{K^t}{K^{t-1}}\right) + \ln\left(\frac{A^t}{A^{t-1}}\right)$$

Annotations in blue boxes:

- Cost share of labour** ( $s_L$ ) is connected to the coefficient of the labour input term.
- Cost share of capital** ( $s_K$ ) is connected to the coefficient of the capital input term.
- % change in output** is connected to the left side of the equation,  $\ln\left(\frac{Q^t}{Q^{t-1}}\right)$ .
- % change in labour input** is connected to the labour input term,  $\ln\left(\frac{L^t}{L^{t-1}}\right)$ .
- % change in capital input** is connected to the capital input term,  $\ln\left(\frac{K^t}{K^{t-1}}\right)$ .
- % change in MFP** is connected to the right side of the equation,  $\ln\left(\frac{A^t}{A^{t-1}}\right)$ .

# MFP and labour productivity

- Useful tool – decomposition of labour productivity

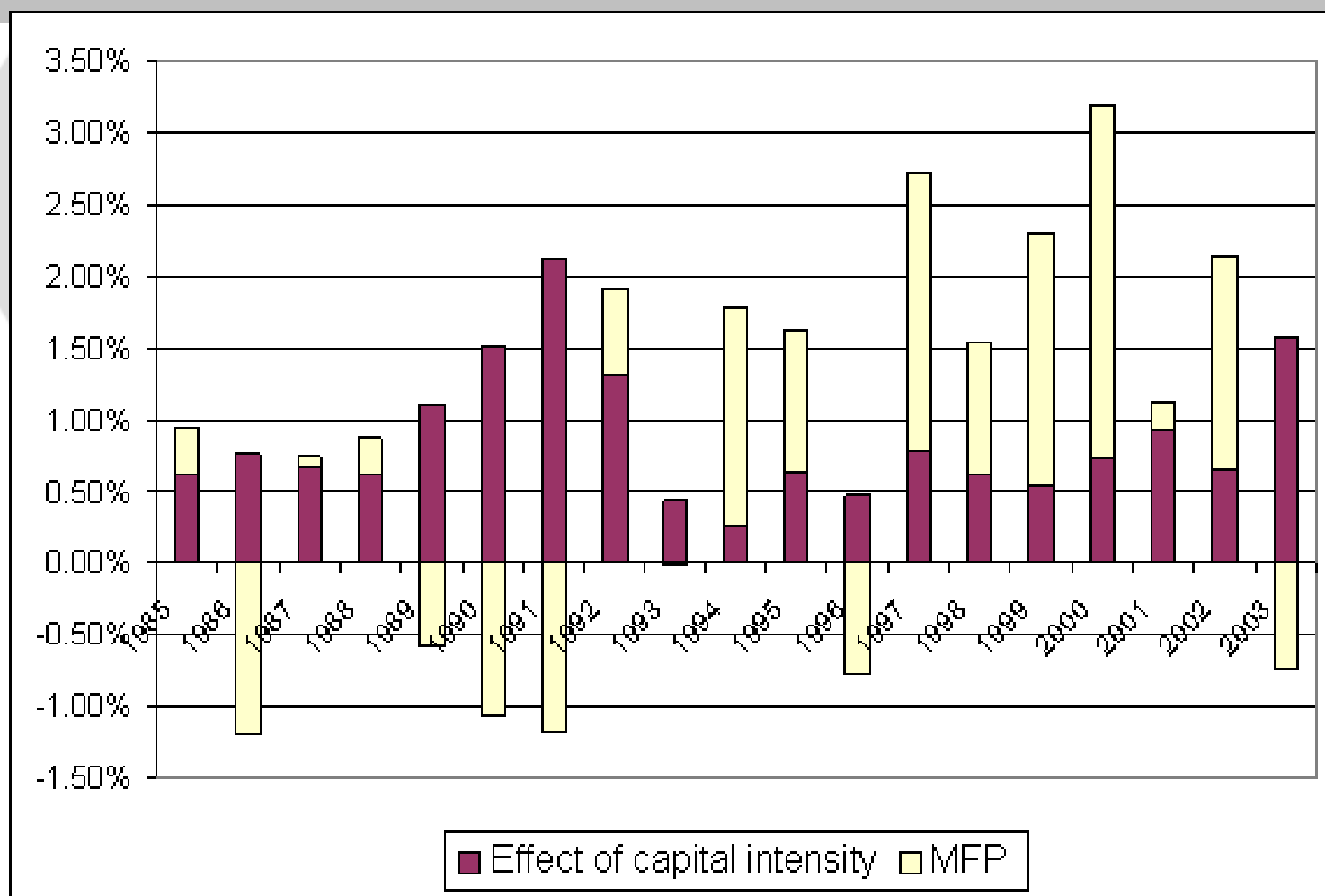
$$\underbrace{\ln\left(\frac{Q^t}{Q^{t-1}}\right) - \ln\left(\frac{L^t}{L^{t-1}}\right)}_{\% \text{ change labour productivity}} = (1 - s_L) \underbrace{\left( \ln\left(\frac{K^t}{K^{t-1}}\right) - \ln\left(\frac{L^t}{L^{t-1}}\right) \right)}_{\text{Effect of capital intensity}} + \underbrace{\ln\left(\frac{A^t}{A^{t-1}}\right)}_{\text{Effect of MFP}}$$



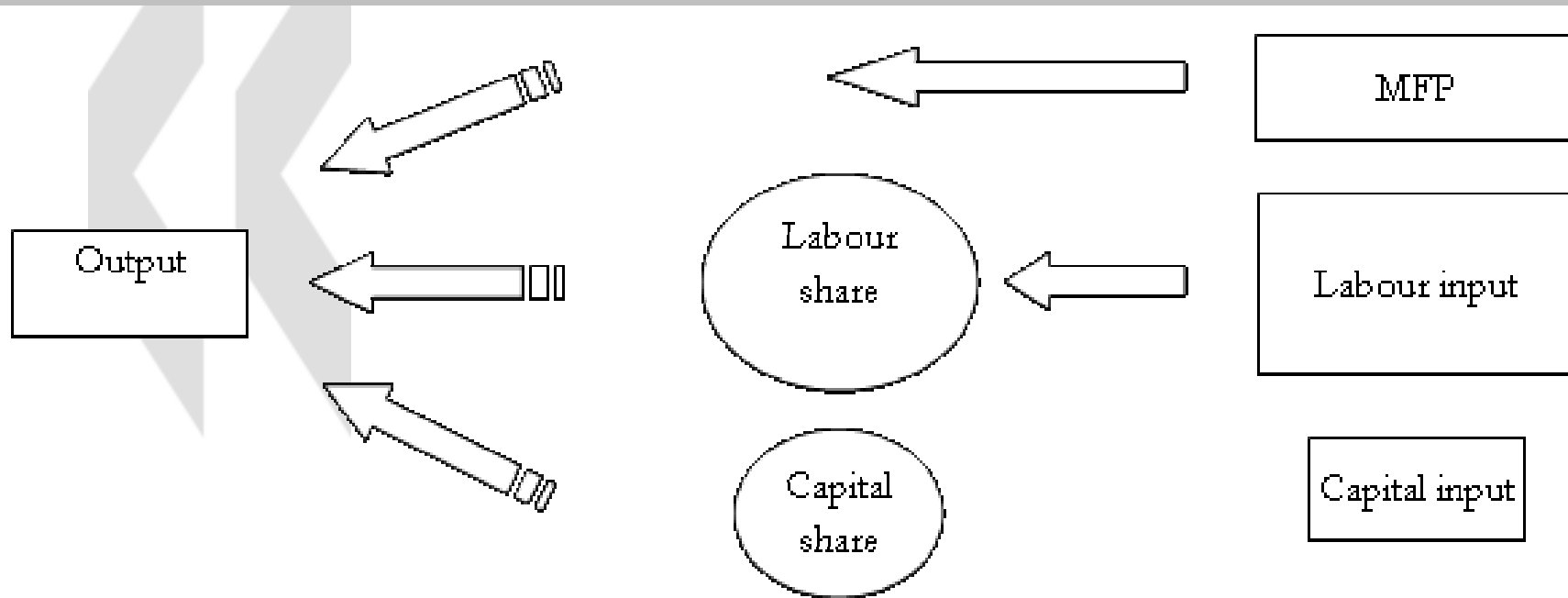
# MFP and labour productivity

- Decomposition of labour productivity important:
  - Is labour productivity driven by investment in ‘traditional’ capital (--> rise in capital intensity)?
  - Is labour productivity driven by investment in ‘intangible’ capital, i.e., innovation, organisational change, R&D (--> change in MFP)
- Example: Canada

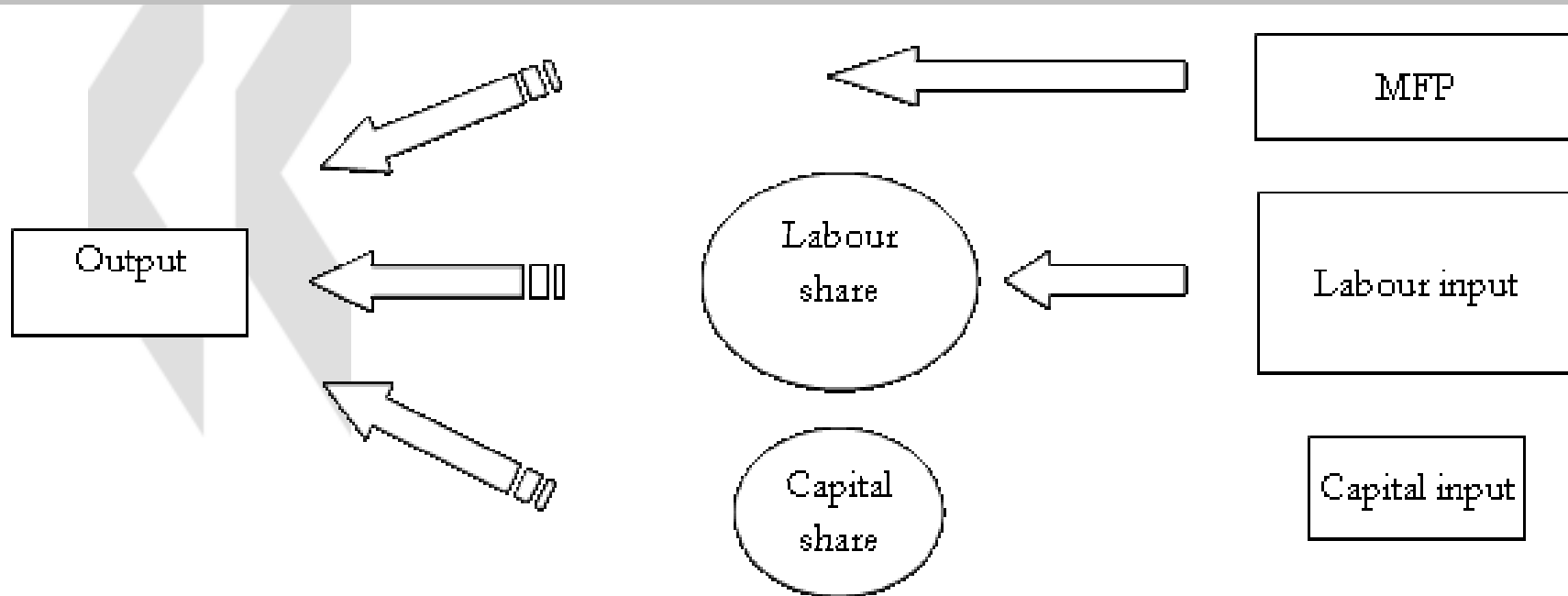
# Decomposition of labour productivity, Canada



# MFP – framework



# MFP framework: measurement issues



**Tricky areas:**  
-Implicit pricing  
-Non-market services  
-Quality change

# Measuring output: 3 tricky areas

- 1) Output measures for industries where there is implicit pricing so that even *nominal* output measures are debated:
  - Banking (FISIM, how to deal with new financial instruments and risk?)
  - Insurance (how to deal with catastrophes?)
  - ➔ OECD Taskforce recommends to measure insurance output as premiums minus *expected* claims, not actual claims
  - ➔ Otherwise sharp drop in output when there is a catastrophe

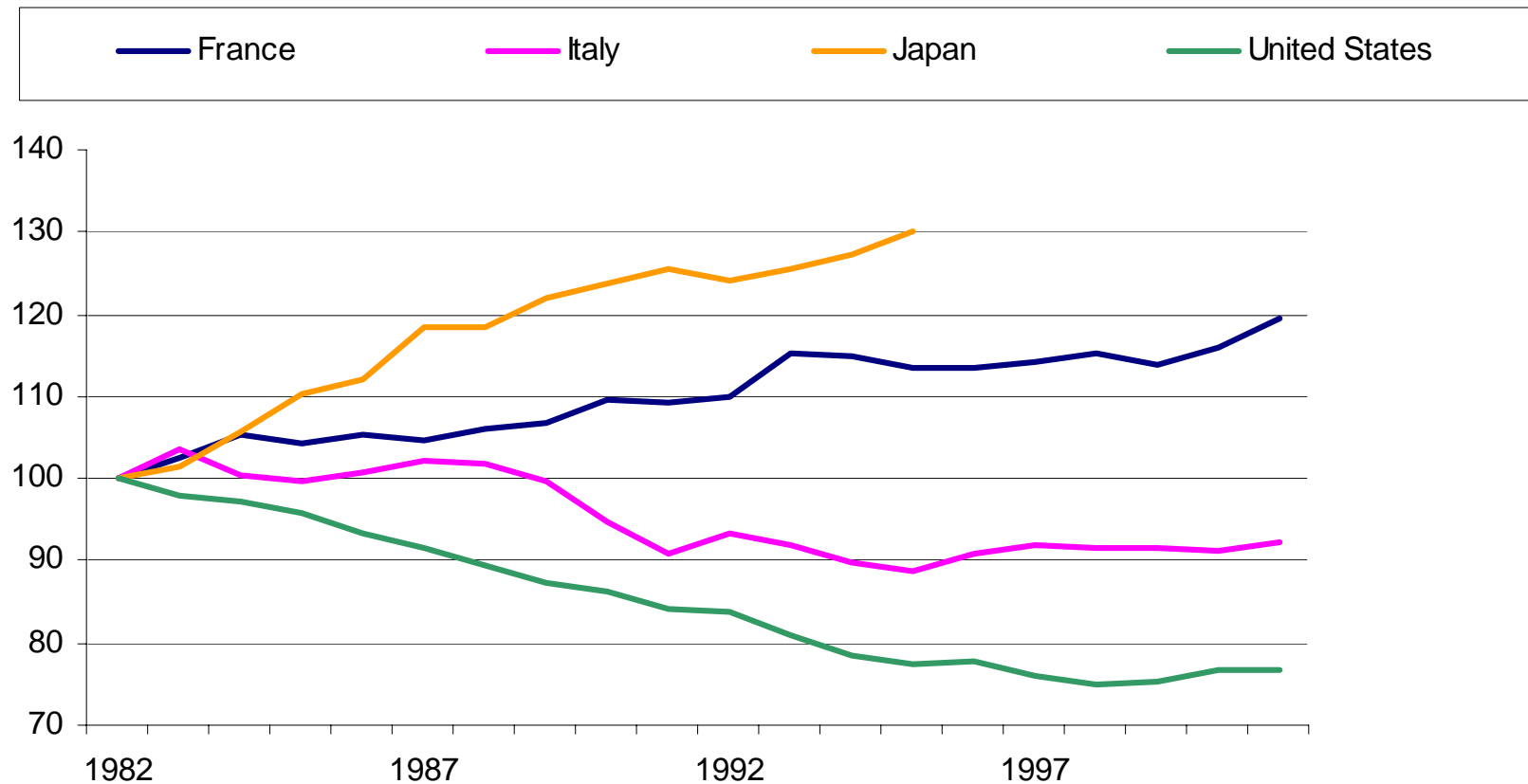
# Measuring output: 3 tricky areas

- 2) Output measures for industries where technology moves fast and where rapid quality change makes price measurement difficult
  - Example ICT: computer production, communication services
  
- 3) Output measures for industries with non-market producers
  - Traditionally from input side
  - But increasingly demand for output-based measures → *Atkinson Report UK*

# Measuring output: 3 tricky areas

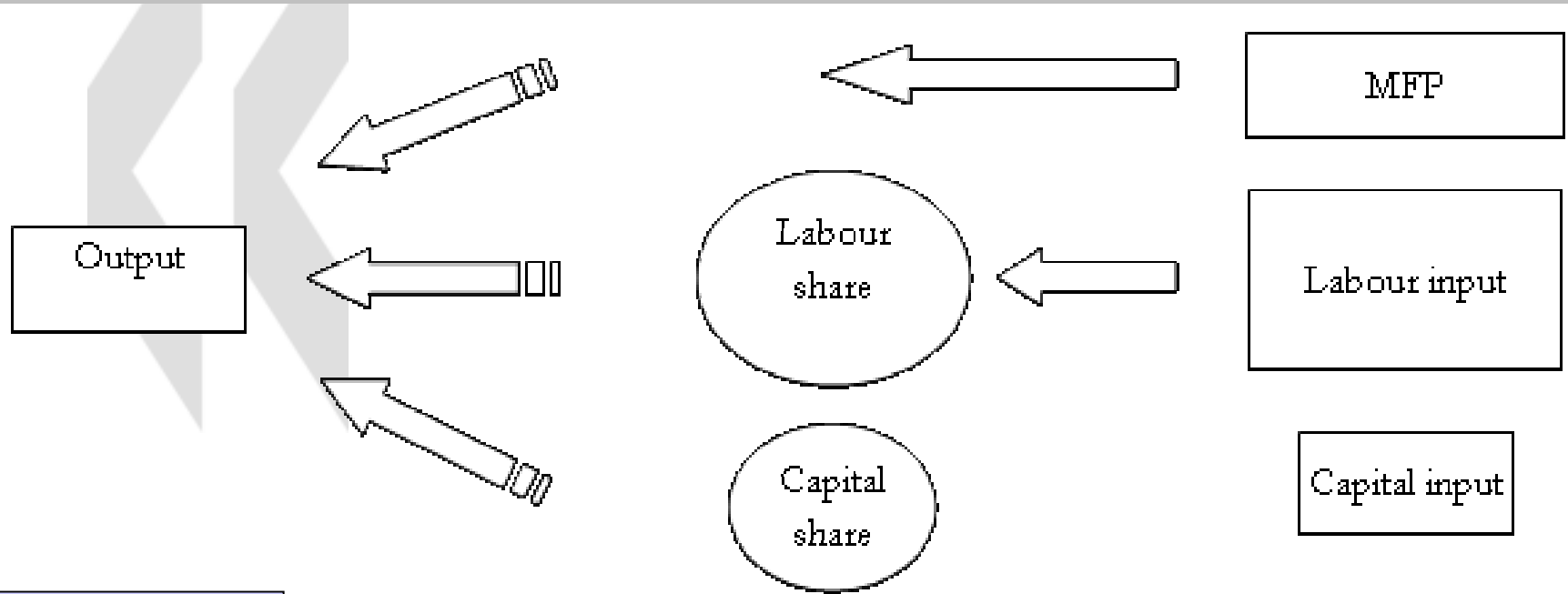
**Chart 5. Real value added per employed person in the health and social work industry**

Indices, 1982=100



Source: OECD.

# Multi-factor productivity framework: measurement issues



## Comparability of GDP growth rates:

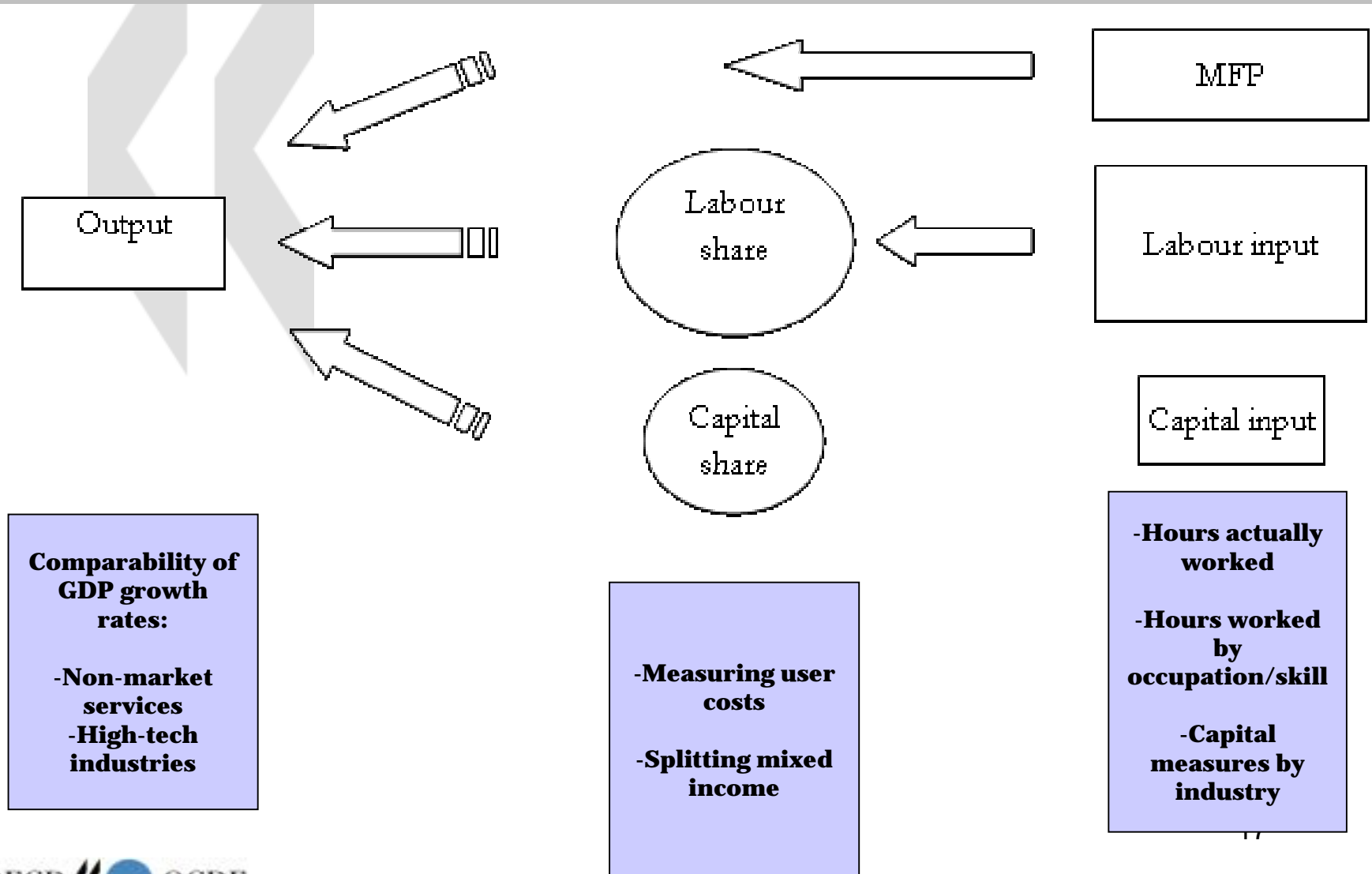
- Non-market services
- High-tech industries

## Measuring user costs

## Splitting mixed income



# Multi-factor productivity framework: measurement issues

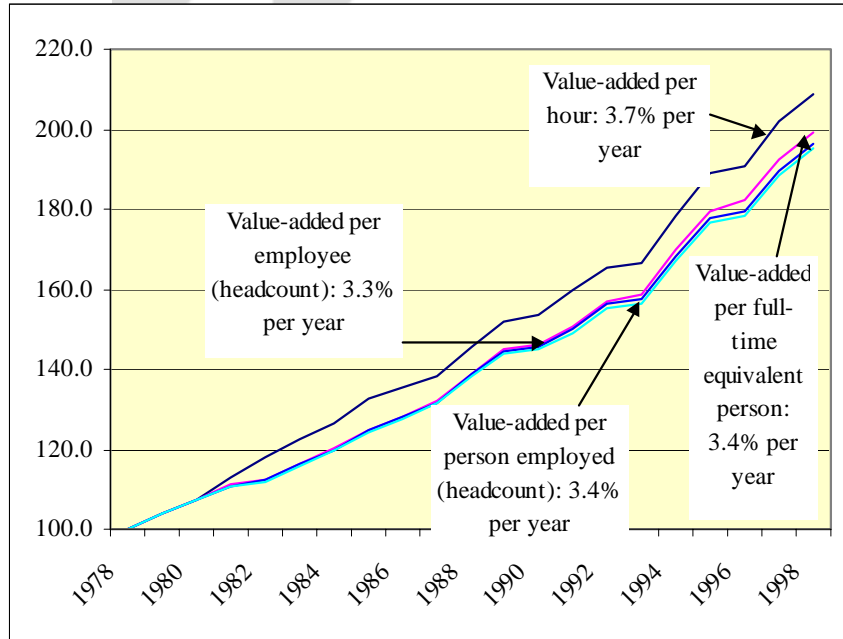


## 4. Measuring labour input

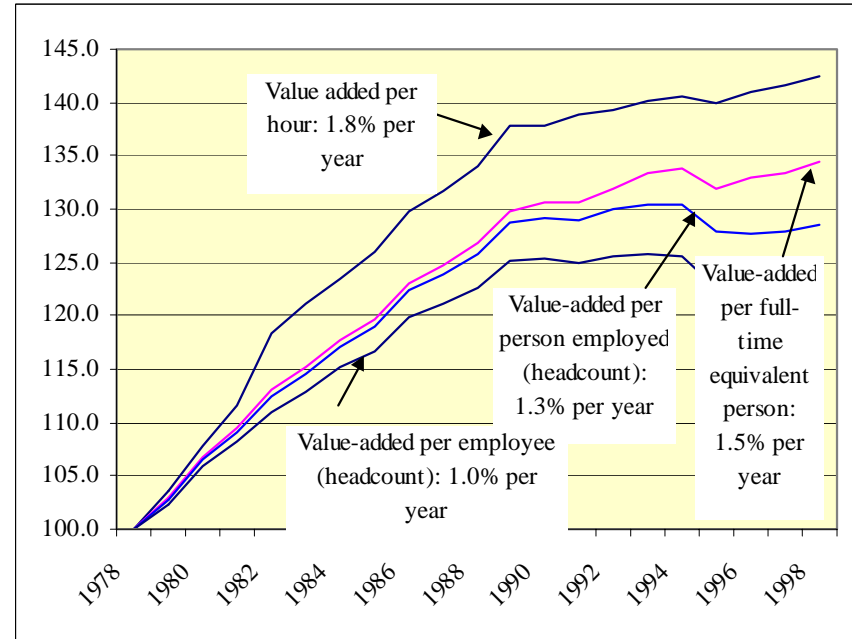
- Ideal measure: total number of hours worked, broken down by type of labour input
- Number of persons employed or number of jobs can generate biased measures of productivity if hours per person change or if there are multiple job holdings
- Total hours should comprise the hours of employees, the hours of self-employed and the hours of unpaid workers (e.g. family members in agriculture)

# Example: impact of different measures of labour input on labour productivity, France

## Industry (mining, manufacturing and construction)



## Market services



\*Output is measured as a quantity index of value-added.

# Labour input: statistical issues

*1) Two main statistical sources* for hours worked:

- Labour force surveys (LFS)
- Establishment or firm-based surveys (ES)
- Results are not normally consistent

➔ Important role for national accountants:

Bring together these sources and provide labour input measures by industry (and sector) that are consistent with output measures

# Labour input: statistical issues

## 2) *Splitting mixed income:*

- Important for productivity measurement: how big is labour income?
- To date: crude approximations are made
- ➔ National accounts could help by putting forward higher quality estimates

## 3) *Information on composition of hours worked and relative remuneration:*

- What is skill composition of hours?
- What is the wage difference between  $n_1$  skill levels?

# 5. Measuring capital input

- Conceptually correct measure: capital services (Theory see Griliches, Jorgenson, Diewert)
- Capital services = flow of productive services that capital delivers in production
- Measurement assumption: capital services = fixed proportion of productive capital stock

# Productive capital stock of a particular asset type

$$K_t = I_t + h_1 I_{t-1} + h_2 I_{t-2} + \dots + h_T I_{t-T}$$

Past  
investment

Efficiency and  
retirement parameter

# Capital services of a particular asset type

Growth of capital services of a particular asset type =  
Growth of productive stock of this asset type

$$\ln\left(\frac{S_t}{S_{t-1}}\right) = \ln\left(\frac{K_t}{K_{t-1}}\right) \quad \text{because} \quad S_t = \lambda K_t$$

Normally assumed as  
constant



# Price of capital service = user costs

How much would the owner of a capital good charge in a competitive market to rent the capital good out for one period (Diewert 1974)?

$$u_t = (r_t + \delta_t - i_t)p_t$$

Rental price  
or user cost

Required rate  
or return

Rate of  
depreciation

Rate of asset  
price change

# Price and quantity of capital services

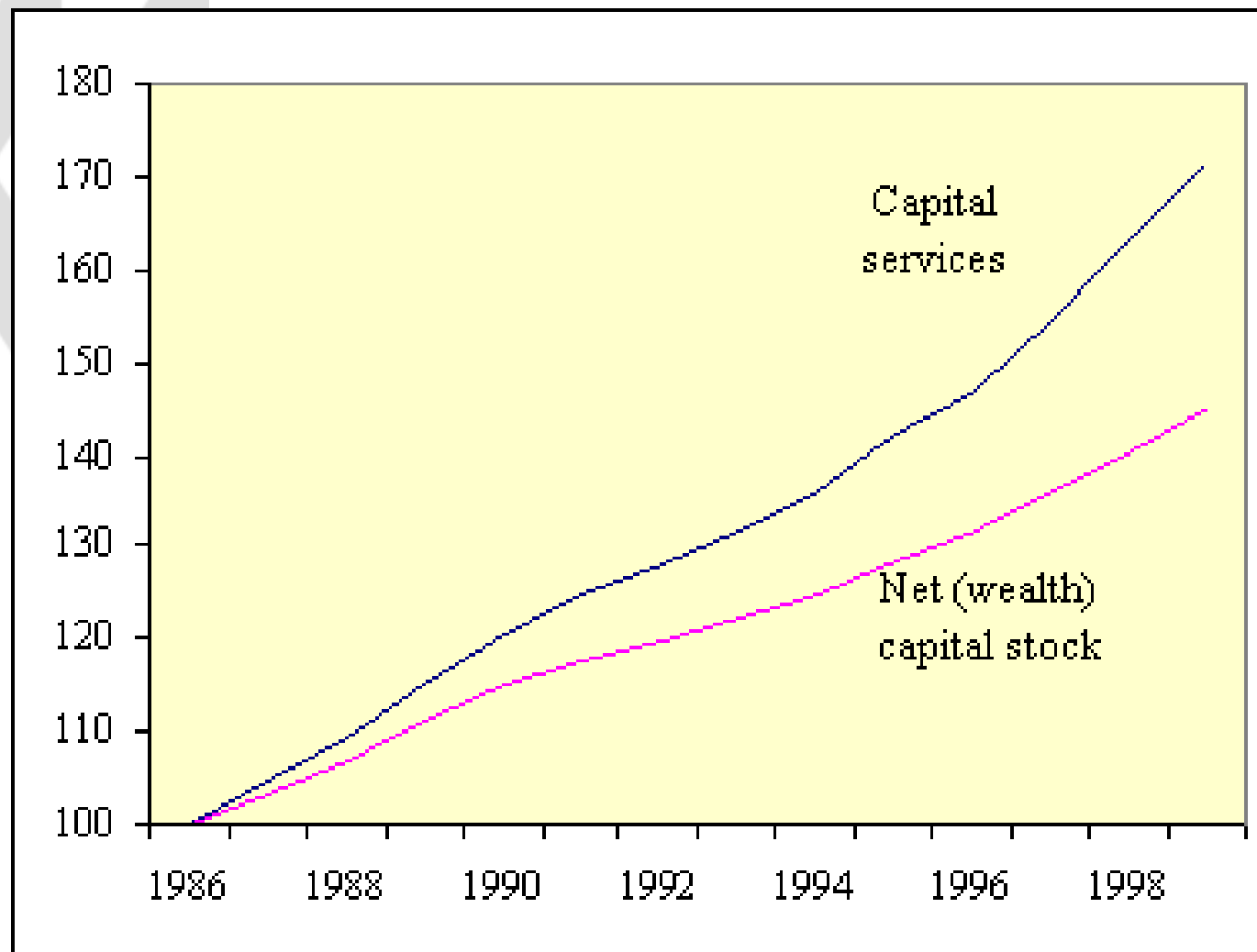
Value of capital services for asset  $i = u_t^i S_t^i$

User costs and the rate of capital service for each asset type are brought together to form an index of overall capital input = the rate of change of total capital services

$$\ln\left(\frac{K^t}{K^{t-1}}\right) = \sum_i w_i^t \ln\left(\frac{K_i^t}{K_i^{t-1}}\right)$$

Average share of each asset in total value of capital services

# Capital services and net capital stock, Australia



# Capital services and national accounts

Capital services are different from net and gross capital stock

*But different does not mean unrelated*

*Desirable:* consistent entity of

- Net capital stock and balance sheets
- Productive stock and capital services
- Consumption of fixed capital (=depreciation)

This is one important topic of SNA revision, discussed next week in Canberra by Canberra II Group

# Capital services and national accounts

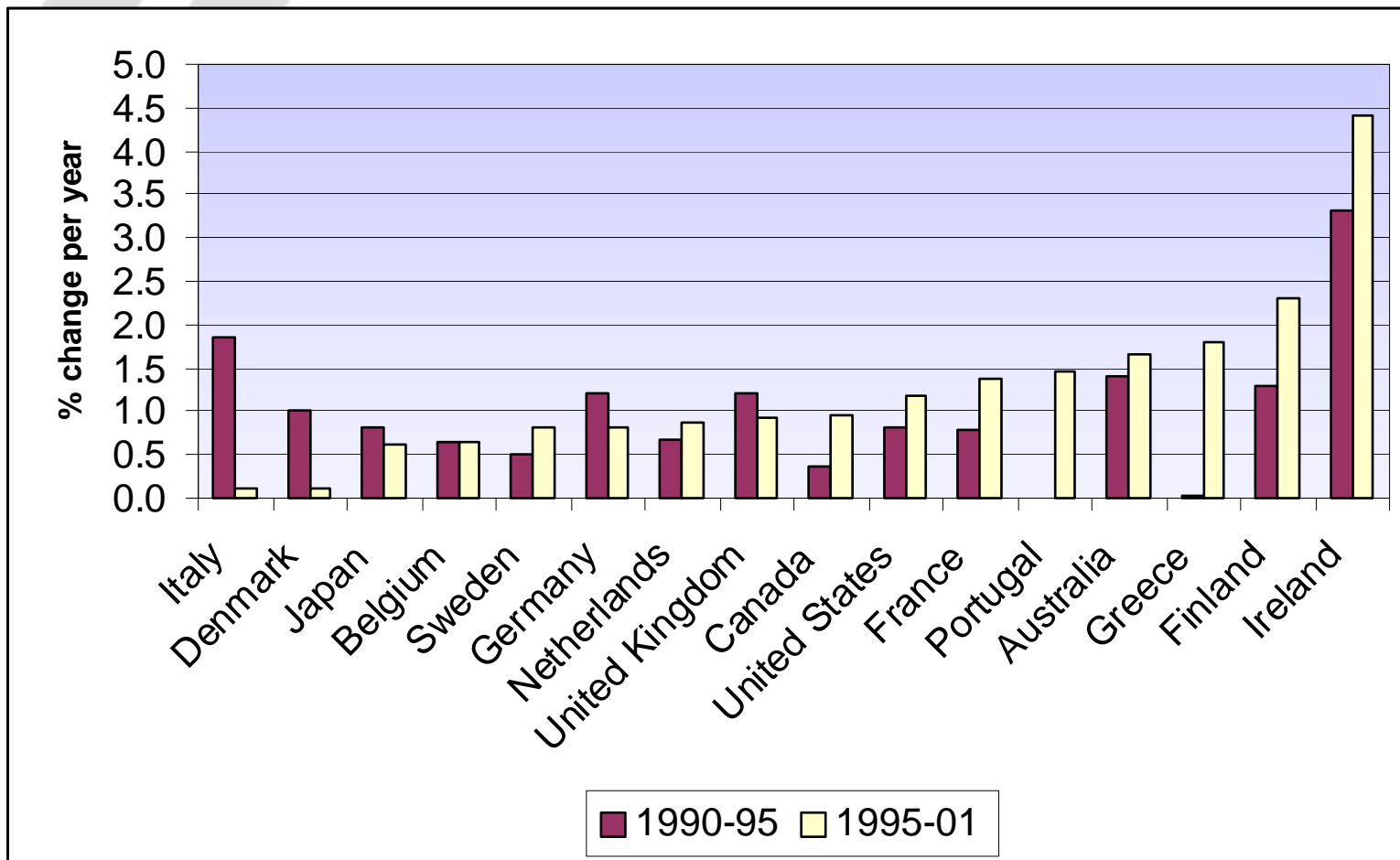
Some measurement issues:

- Availability and quality of investment series
- Breakdown by type of asset important
- Scope of assets
- Investment deflators

## 6. OECD Productivity database

- Since March 2004, OECD productivity data available on the internet:
- [Productivity:Statistics Portal](#)
- For total economy:
  - Growth of GDP, hours worked and capital services
  - Labour productivity growth
  - MFP growth
  - Labour productivity levels

# Average rates of MFP growth



# 7. OECD Factbook

- Since last week: OECD Factbook
- **Online version** is freely available at <http://new.SourceOECD.org/factbook> and enables the downloading of the data underlying the tables and graphs
- First compilation of economic, social and environment indicators across OECD countries
- Chapter on macro-economic indicators includes productivity comparisons, in particular MFP growth rates



## 8. Conclusions

- Productivity is a key indicator for analysis of economic growth --> significant demand from policy makers
- Simple ratio but sometimes difficult to measure
- Desirable: close integration of productivity measures and their ingredients with the national accounts
- Release of ‘official’ productivity statistics by statistical agencies



**Thank you for your attention!**